### ABCD input impedance model





Considering dominant pole only  $K_V(s) = \frac{\kappa_V}{1 + s \cdot \tau_{PO}}$ the open loop gain is:



And the input impedance in operator domain:

$$Z_{in}(s) = \frac{Z_F(s)}{1 + K_V(s)} \approx \frac{Z_F(s)}{K_V(s)} = \frac{R_F \cdot (1 + s \cdot \tau_{P0})}{K_V \cdot (1 + s \cdot \tau_f)}$$

For ABCD3T preamplifier:

Rf=80k, Cf=120fF  $\rightarrow \tau_{f}$  = 10ns

The Kv and  $\tau_{00}$  we obtain from AC Spice simulation for a given input transistor bias Ic

lc	100uA	200uA	300uA
τ <sub>p0</sub> [ns]	100	53	40
Kv [V/V]	1733	1654	1550

For intermediate values of bias current one should use interpolation function

### ABCD input impedance model



For Ic values from 100 to 300uA range one can approximate the  $\tau_{p0}$  and Kv as following:

$$\tau_{P0} = 181 - 0.98 \cdot I_C + 0.0017 \cdot I_C^2$$
$$Kv = 1829 - 0.915 \cdot I_C$$

where Ic in uA,  $\tau_{p0}$  in ns, and Kv in [V/V]

### ABCD input impedance model

In frequency domain the Zin is following :

$$|Z_{in}| = \frac{R_F}{K_V} \cdot \frac{\sqrt{1 + \omega^2 \cdot \tau_{P0}^2}}{\sqrt{1 + \omega^2 \cdot \tau_f^2}}$$

This simple model using extracted parameters Kv and  $\tau_{p0}$  (left figure) can be verified with the Spice simulation of the ABCD3T input impedance (right) for the same input transistor bias currents



### Currents at front end inputs



Unfortunately the use of this expression gives problems later during calculation of inverse Laplace functions. We have to simplify the model.

### Currents at front end inputs

A reasonable trade off between accuracy and simplicity is shown below:



In this case we assume that input of the preamplifier is loaded with  $c_b$  and two  $c_{is}$  capacitances (neglecting input impedances of the neighbors). Using Kirchhoff law one can write:

$$i_d = u_{in} \cdot \left( s \cdot (c_b + 2 \cdot c_{is}) + \frac{1}{Z_{in}} \right)$$

Since we assume delta Dirac input we can write expression for voltage at the preamplifier input:  $Z_{in}$ 

$$u_{in} = \frac{Z_{in}}{1 + s \cdot (c_b + 2 \cdot c_{is}) \cdot Z_{in}}$$

#### Currents at front end inputs

Expressions for current flowing into the input of readout channel:

$$i_s = u_{in} \cdot \frac{1}{Z_{in}}$$

For the expression of current flowing into neighboring channel we use simplified expression for  $u_{in}$  and expression for input impedance of neighboring channel connected in series with  $c_{is}$  capacitance (neglecting  $c_b$ ):

$$i_c = u_{in} \cdot \frac{1}{Z_{in} + \frac{1}{s \cdot c_{is}}}$$

# Currents at front end inputs; what is happening to signal charge

Current flowing into the input of neighboring channels and backplane capacitance:

$$i_{lost} = u_{in} \cdot s \cdot (c_b + 2 \cdot c_{is})$$

One should note than the overall charge transfer to readout channel is full i.e.

$$\int_{0}^{\infty} i_{s}(t) \,\partial t = 1 \quad and \int_{0}^{\infty} i_{lost}(t) \,\partial t = 0$$

That means that after some delay caused by Zin all charge flows finally into the input of preamplifier connected to the hit strip i.e. we do not see the loss of charge however the response of the preamplifier stage is generally slower due to extra time constant created by Zin and detector capacitance (detector time constant).

In general the detector time constant modifies the preamplifier transfer function changing the gain, peaking time and phase margin. All those changes and possible loss of signal at the end of the full signal processing chain will depends on detector time constant and time constants of all stages contributing to the signal formation.

N.B. This applies to transimpedance preamplifiers, where the input impedance has real part. In case of pure charge preamplifier with non-continuous reset (reset switch) there will be real charge sharing in between all capacitances at the preamplifier input during the readout phase.

## ABCD transfer function and responses to signal and crosstalk

Overall transfer function of ABCD3T channel can be approximated with CR-RC response of preamplifier with time constant of  $\tau_f$  = 10ns and two stages of integrators with time constant  $\tau_i$  = 4ns

$$T_{ABCD} = \frac{\tau_f}{\left(1 + s \cdot \tau_f\right)^2} \frac{1}{\left(1 + s \cdot \tau_i\right)^2}$$

The response of ABCD to delta Dirac function in time domain will be:

 $L^{-1}(T_{ABCD}\cdot i_s)$ 

The crosstalk of first neighbor in time domain will be:

$$L^{-1}(T_{ABCD}\cdot i_c)$$

### Example of calculation

Kv and  $\tau_{\rm p0}$  for Ic=200uA (table page 1)



Response for channel not loaded with detector

Max=0.313349 for t=19.4366ns

### Example of calculation

Kv and  $\tau_{p0}$  for Ic=200uA (table page 1),  $c_b$ =4pF,  $c_{is}$ =7pF



Response for channel loaded with detector

Max=0.34299 for t=23.7339ns

When compare to response of the open channel (previous page) we can see that the peaking time has been changed from 19.4ns to 23.7ns and the peak gain has been increased from 0.313 to 0.343. The change of gain and peaking time is caused by detector time constant which change the overall response of the preamplifier (modifying also the phase margin).

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Crosstalk
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Max=0.0339311 for t=12.012ns

# Comparison of analytical model to Spice simulations

Crosstalk for cis=7pF and cb=4pF and Ic=200uA calculated using presented formulas is in the range of 10%.

Crosstalk simulated in Spice for the same detector and front end parameters is in the range of 8% (see figure below). The overestimation of the crosstalk can be both to analytical model inaccuracy as well as to the fact that in the Spice we have used longer charge collection times (8ns) when in calculation we use as the detector signals delta Dirac function.

